



## Math 415: Applied Linear Algebra (3 credit hours)

### Course Description

This is an introductory course emphasizing techniques of linear algebra with applications to engineering. Topics for this course include matrix operations, determinants, linear equations, vector spaces, linear transformations, eigenvalues and eigenvectors, inner products and norms, orthogonality, equilibrium, and linear dynamical systems.

Prerequisite: Calculus III

### Course Objectives

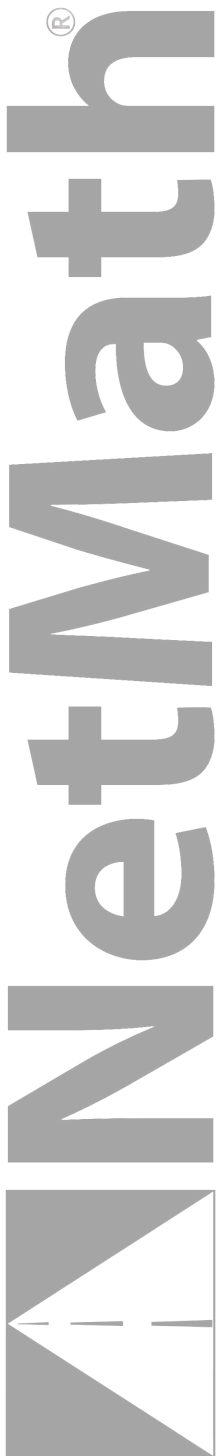
After completing this course a successful student will be able to understand and apply the topics listed above. He/she will also be able to apply numerical, computational, and estimation techniques. Through exploration, a successful student will be able to use matrices to model and analyze physical phenomena. He/she will also have the necessary tools to formulate and solve problems in mathematical situations and connect concepts to other disciplines. Most importantly, a student completing this course will be able to communicate ideas through descriptive language as well as mathematical symbols.

### Course Content and Format

#### *Content*

A brief outline of topics for this course appears below:

- Perpendicular Frames
  - Vector operations and dot product
  - Hanging and aligning curves in 2D and 3D space
  - Area, Volume, and cross product
- 2D Matrix Action
  - Identity and Stretching matrices
  - Matrix rotations and operations
  - Using hangers, stretchers, and aligners to create matrices
  - Positive definite, reflection, inverse, and transpose matrices
- SVD Analysis of 2D Matrices
  - Inverting a 2D matrix
  - Rank of a matrix and properties of the determinant



- Cramer's Rule
- 3D Matrices
  - Finding rank, determinants, and rotations
  - Using SVD analysis to invert a 3D matrix
  - Matrices for bouncing light rays off surfaces
  - Gaussian elimination and reduced row echelon form
- Ill-conditioned Matrices and Roundoff
  - Principal Component Data Analysis via SVD
  - Creative rounding of matrices and image compression
- Properties of Matrices
  - Subspaces and spans
  - Linear independence and dimension
  - Orthonormal bases
- Eigensense
  - Diagonalization of a Matrix
  - Properties of eigenvalues and eigenvectors
  - Dynamical systems
- The Spectral Theorem
  - Applications of the Spectral Theorem
  - Gradient vectors
- Function spaces and Root-Mean Square Approximation
  - Orthogonal sets of functions
  - Fourier Approximations
  - The Gram-Schmidt Process

*Format*

Course content is drawn from *Matrices and Geometry* written by Bill Davis, Horacio Porta and Jerry Uhl ©2006-2010.

Math 415 utilizes the CAS-ILE system. See <https://cas-ile.illinois.edu/> for more information. This online system helps students learn math topics through dynamic exploration and visualization.

Exams for Math 415 are taken online.

