



Math 447: Real Variables

Offered through **NetMath[®]**

Academic Year 2026-2027 Term, 16-week course

Instructor Information

Instructor – Jason Elliot

- Contact information: jelliot2@illinois.edu or math447@netmath.illinois.edu
- Office hours announced weekly via Canvas.

Course Information

Credit Hours

3 credit hours

Course Description

Careful development of elementary real analysis for those who intend to take graduate courses in Mathematics. Topics include completeness property of the real number system; basic topological properties of n -dimensional space; convergence of numerical sequences and series of functions; properties of continuous functions; and basic theorems concerning differentiation and Riemann integration.

Prerequisite

MATH 241; MATH 314 or MATH 347

Course Objectives:

Introduction to real analysis is a gateway. The idea is to find balance between rigorous proofs and real understanding. This principle is the core of mathematics at all levels. Be prepared to learn to write proofs. Be prepared to accept a little abstract but clarifying approach to well known, and not so well known topics related to calculus.

Course Content:

1. Real Numbers: Natural numbers, Abelian groups, Grothendieck's construction, Integers, Fields, Rational numbers, Ordered fields, Completeness, Peano's axiom, Uncountability of real numbers.
2. Sequences: Limits, Monotone sequences, Subsequences, Bolzano-Weierstrass, Limsup and liminf, Application to continuous functions
3. Metric Spaces: Metric spaces, Cauchy sequences, Completeness, Sequential compactness and total boundedness, Open, closed and compact sets, Application to Heine-Borel and continuity of inverses, Connected sets Intermediate value theorem.
4. Spaces of Continuous Functions: Uniform continuity, $C(K)$ is a complete metric space, Dini's theorem, application, Interchanging differentiation and limit.
5. Differentiation: Rolle's lemma and the mean value theorem, Differentiation of power series.
6. Integration: Definition, Interchanging limits, Fundamental theorem and application to power series.

Course Structure:

This course is fully online and asynchronous. Students have 16 weeks from their course start date to complete the course. The course is self-paced, and students may complete their coursework prior to the assigned end date. However, students are encouraged to follow the guided structure provided by the instructor with suggested deadlines for assignments and exams. As this is a 3-credit hour course, students are expected to dedicate 9 hours per week to learning course content.

Students should complete roughly one unit per week, with about a week dedicated to each exam as well. This is a rough average and students can certainly move at different paces at different parts of the course. There are 13 homeworks (one for each unit), which collectively determine 20% of their final grade. Each exam is also weighted 20%. Canvas is the platform used for this course, which includes all lectures, notes, and assignments.

When working on a particular unit, the best approach is to watch each of the lectures and follow along with the respective slides. Make sure each of these is fully understood, as this is the basis of this course. Most students find there are some parts of some lectures that do not fully "click" at first. Spend some time on these parts. Try to see why each claim the lecturer makes is true and why it is relevant (how it leads to the desired result). My office hours and email conversations are a very good place for consulting me for guidance.

Students should be prepared to prove things in this course and to think rigorously about theorems they may have already been taught (in calculus, for example). We begin with a first-principles approach to constructing the real number system before analyzing functions of a real variable. This is all done with rigor, so students should have the appropriate level of "mathematical maturity." Students should be prepared to "formally forget" what they have been taught about this subject so that these properties can be established rigorously.

Exams:

Information	Exam 1	Exam 2	Exam 3	Final Exam
Coverage:	Unit 1-5	Unit 6-8	Unit 9-12	Comprehensive
Time Limit	90 Minutes	90 Minutes	90 Minutes	3 Hours

All exams will be administered online, free of charge to students. Exams are administered using ProctorU Record+. [More information on taking exams.](#)

Calculators are not permitted or required for NetMath exams.

The use of outside sources is prohibited.

Refer to the Academic Integrity policies below in the syllabus for more details.

Scratch paper is allowed during exams.

Exams must be taken in course order and students should not take more than 1 exam within a 24-hour period.

Grading:

Grading Breakdown:

Component	Weight
Homework	20%
Exam 1	20%
Exam 2	20%
Exam 3	20%
Final Exam	20%

Letter Grade Scale:

Percentage	Letter Grade
97 - 100	A+
93 - 96	A
90 - 92	A-
87 - 89	B+
83 - 86	B
80 - 82	B-
77 - 79	C+
73 - 76	C
70 - 72	C-
67 - 69	D+
63 - 66	D
60 - 62	D-
59 and below	F

Final grades are rounded to the nearest integer before applying the scale above.
Grades are not curved.

Once you complete your exam, you will receive a 0 on any homework leading up to that exam that has not been submitted. Under special circumstances, students may request that they be allowed to submit these assignments. This is left to the discretion of the course instructor.

Students are encouraged to follow the guided deadlines in their course. However, as our courses are self-paced, students may occasionally submit several assignments in a short period of time. Please note that instructors are only expected to grade one exam per five-business-day week, and instructors are only expected to grade up to two submitted assignments per five-business-day week. Under special circumstances, students may request that additional assignments be graded. This is left to the discretion of the course instructor.

Due to the rolling enrollment structure of the NetMath program, instructor workloads vary throughout the year. During peak periods, response times and grading turnaround may be longer than usual. Students should expect significant delays in grading and instructor responses between June and August.

Communication:

You may reach out to the instructor via email or attend office hours.

If you experience consistent and significant delays in reaching your instructor, please contact instruction@netmath.illinois.edu with your concerns.

If you have non-course specific questions, you may reach out to the NetMath office. It is recommended to [review the NetMath website](#) first as it often has the answers you need.

General Inquiries: netmath@illinois.edu

Proctoring Questions: proctor@netmath.illinois.edu

Technology Questions: tech-staff@netmath.illinois.edu

Main Office Phone: [\(217\) 265-0439](tel:(217)265-0439)

Phone hours: Monday - Friday, 9am - 12pm & 1pm - 4pm CST

Textbook:

Required:

Kenneth Ross. (2013). Elementary Analysis: The Theory of Calculus (2nd Edition). Springer.

Recommended Textbook:

R. Creighton Buck. Advanced Calculus (3rd Edition)

- A very good book at roughly the same level as our course with different areas of focus. This is a good source of examples and exercises and contains explanations that are not in our textbook or the lectures.

Walter Rudin. Principles of Mathematical Analysis

- A more advanced book that covers the same material. It is a (the) classic textbook on this subject.

Technical Requirements:

Students are expected to have a device with an up-to-date operating system to access their course materials, reliable internet access, and must meet the requirements set by ProctorU for exam proctoring. [NetMath IT - Frequently Asked Questions](#).

Other Information:

This course features video lectures from the UIUC Spring 2018 course taught by Professor Marius Junge.

Policies:

Accommodations:

The University of Illinois Champaign-Urbana, is committed to ensuring that all students, including students with disabilities, do not experience barriers to learning and participating fully in class. Students who have a letter of accommodation from DRES are advised to share that with their instructor and NetMath staff at instruction@netmath.illinois.edu as soon as possible to ensure accommodation needs can be discussed and met.

Students enrolled in a degree program at another institution may refer to their home institution's student services or disability office for accommodations. Current, non-expired documentation from other institutions listing the specifics of an accommodation is acceptable and should be sent to instruction@netmath.illinois.edu.

To obtain disability-related academic accommodations, disabled students must contact Disability Resources and Educational Services (DRES) as soon as possible. To contact DRES, please visit 1207 S. Oak Street, Champaign, call [\(217\) 333-1970](tel:(217)333-1970), email disability@illinois.edu, or [visit the DRES website](#).

Academic Integrity:

The University of Illinois Urbana-Champaign [Student Code](#) (<https://studentcode.illinois.edu/>) should also be considered as a part of this syllabus. Students should pay particular attention to Article 1, Part 4: Academic Integrity.

Academic dishonesty may result in a failing grade. Every student is expected to review and abide by the [Academic Integrity Policy](#) (<https://studentcode.illinois.edu/article1/part4/1-401/>). Ignorance is not an excuse for any academic dishonesty. It is your responsibility to read this policy to avoid any misunderstanding. Do not hesitate to ask the instructor(s) if you are ever in doubt about what constitutes plagiarism, cheating, or any other breach of academic integrity.

AI Large Language Models (such as ChatGPT, Claude, Gemini, etc.) are prohibited during exams. Using these during the exam will be considered a violation of academic integrity and may incur sanctions as outlined in the Illinois Student Code. Students should be aware the exam proctoring process involves screen recording of the computer. While AI will not be strictly prohibited for homework as they can be useful tools for studying and brainstorming, students are strongly encouraged to work on the homework themselves or collaborate with peers when appropriate. Students are required to submit their own work and answers. This improves learning outcomes and best prepares students for exams. Homework is designed to help students understand the content and develop skills. Students may be unprepared for exams if there is heavy reliance on AI.

Students are expected to follow the [University guidance on intellectual property](#). Students are not to share course content outside of the course.

Campus Holidays:

Instructors are expected to respond to student communications and grade homework assignments in a timely manner. Observed Campus Holidays, illness, personal obligations, or other circumstances outside the instructor's control may affect normal grading and response time. If you experience consistent and significant delays, please contact instruction@netmath.illinois.edu with your concerns.

Extensions:

Students in this course are eligible for up to two 1-month course extensions. There is a non-refundable \$350 fee for each approved extension. [Students should review the extension guidelines for more information](#).

FERPA:

See [FERPA – Office of the Registrar](https://registrar.illinois.edu/academic-records/ferpa/) (<https://registrar.illinois.edu/academic-records/ferpa/>) for more information on the Family Educational Rights and Privacy Act (FERPA).

Any student who has suppressed their directory information pursuant to FERPA should self-identify to the instructor to ensure protection of the privacy of their attendance in this course.

Mental Health:

Significant stress, mood changes, excessive worry, substance/alcohol misuse or interferences in eating or sleep can have an impact on academic performance, social development, and emotional wellbeing. The University of Illinois offers a variety of confidential services including individual and group counseling, crisis intervention, psychiatric services, and specialized screenings which are covered through the Health Service Fee. If you or someone you know experiences any of the above mental health concerns, it is strongly encouraged to contact or visit any of the University's resources provided below. Getting help is a smart and courageous thing to do for yourself and for those who care about you.

[Counseling Center](#) or [\(217\) 333-3704](#)

[McKinley Health Center](#) or [\(217\) 333-2700](#)

[National Suicide Prevention Lifeline](#) or [\(800\) 273-8255](#)

[Rosecrance Crisis Line](#) or [\(217\) 359-4141](#) (available 24/7, 365 days a year)

If you are in immediate danger, call [911](#).

*This statement is approved by the [University of Illinois Counseling Center](#)

Sexual Misconduct Reporting Obligation:

The University of Illinois is committed to combating sexual misconduct. Faculty and staff members are required to report any instances of sexual misconduct to the University's Title IX Office. In turn, an individual with the [Title IX Office](#) will provide information about rights and options, including supportive measures, resources, the campus disciplinary process, and law enforcement options.

[Designated Confidential Employees](#): A list of the designated University employees who, as counselors, confidential advisors, and medical professionals, do not have this reporting responsibility and can maintain confidentiality.

Other information about [resources and incident reporting](#).