



Math 417: Introduction to Abstract Algebra

Offered through **NetMath**

Academic Year 2026-2027 Term, 16-week course

Instructor Information

Instructor – Jason Elliot

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- Office hours are announced weekly via Canvas.

Course Information

Credit Hours

3 credit hours

Course Description

Fundamental theorem of arithmetic, congruences. Permutations. Groups and subgroups, homomorphisms. Group actions with applications. Polynomials. Rings, subrings, and ideals. Integral domains and fields. Roots of polynomials. Maximal ideals, construction of fields.

Prerequisite

MATH 241; MATH 314, MATH 347, or CS 374

Course Objectives:

Students will begin by looking at binary operations and considering how they give rise to various algebraic structures, then move on to an in-depth study of groups and rings, including special cases of abelian groups, finite groups, domains, fields, PIDs, UFDs and more. Applications and examples of groups and rings will also be considered, including group actions, polynomials, matrices, and applications to number theory.

In addition, students will prove various fundamental theorems and examine homomorphisms.

Course Content:

1. Introduction to abstract algebra, groups and permutations
2. Order of group elements, parity of permutations, permutation matrices, algebraic properties of integers, greatest common divisor, lowest common multiple, well-ordering principle, congruence and modular arithmetic
3. Binomial theorem, Fermat's little theorem, cryptography, abstract groups and properties of groups, group isomorphisms, monoids and semigroups
4. Groups of small order, subgroups, generators of groups, cyclic subgroups, cyclic groups, group homeomorphisms
5. Normal subgroups, cosets, Lagrange's theorem, index of a subgroup
6. Even order theorem, generalized Lagrange theorem, equivalence relations, quotient groups, cycle conjugation of permutations and applications, homomorphism theorem for quotients, first isomorphism theorem and examples
7. Correspondence theorem for isomorphisms, factorization theorem for isomorphisms, product subsets, diamond isomorphism theorem, direct product of groups, Chinese remainder theorem
8. Automorphisms of groups, $\text{Inn}(G)$ and $\text{Out}(G)$, conjugation, center of a group, semidirect products, identification theorems for direct and semidirect products netmath.illinois.edu
9. Finitely generated abelian groups, invariant factors and elementary divisors, free abelian groups, Smith normal form for matrices, linear independence, homomorphisms of free abelian groups
10. Elementary matrices, symmetry groups with examples, orbits, stabilizers, kernel of an action, orbit stabilizer theorem, Cayley theorem, regular action and conjugacy action
11. Centralizers, conjugacy classes, Burnside formula for orbits, finite subgroups of $\text{SO}(3)$
12. Fixed points of an action, fixed point theorem for p -groups, Cauchy's theorem, even order theorem, groups of order pq , rings, subrings, rings with identity, commutative rings, complex numbers, fields
13. Polynomial rings, division algorithm for polynomials over fields, homomorphisms of rings, unital homomorphisms, isomorphisms and

- automorphisms of rings, substitution principle for polynomials over rings, kernels of homomorphisms, ideals
14. Generators for ideals, principal ideals, ideals in polynomial rings over fields, quotient rings, homeomorphism and isomorphism theorems for rings, domains, field of fractions, units and irreducibility in domains, Gaussian integers, norm function, associates in domains
 15. Primes in domains, principal ideal domains, unique factorization domains, Fermat's theorem for sums of two squares, Dedekind's ideal numbers and the development of ideals.

Course Structure:

This course is fully online and asynchronous. Students have 16 weeks from their course start date to complete the course. The course is self-paced, and students may complete their coursework prior to the assigned end date. However, students are encouraged to follow the guided structure provided by the instructor with suggested deadlines for assignments and exams. As this is a 3-credit hour course, students are expected to dedicate 9 hours per week to learning course content.

Exams:

Information	Exam 1	Exam 2	Exam 3	Final Exam
Coverage:	Unit 1 – 5	Unit 6 – 9	Unit 10 – 15	Comprehensive
Time Limit	90 minutes	90 minutes	90 minutes	3 Hours

All exams will be administered online, free of charge to students. Exams are administered using ProctorU Record+. [More information on taking exams.](#)

There is a module devoted to each of these exams. Within the exam module there is a page that reviews the material for the exam, a page for taking that exam, and a page for file uploads that you may use if you have technical trouble uploading your answers within the exam. There are three quizzes in this course. They fall within units 3, 5, and 9. They are taken within Canvas and graded automatically. The time limit for each quiz is 1 hour and they are unproctored.

Calculators are not permitted or required for NetMath exams.

The use of outside sources is prohibited.

Refer to the Academic Integrity policies below in the syllabus for more details.

Scratch paper is allowed during exams.

Exams must be taken in course order, and students should not take more than 1 exam within a 24-hour period.

Grading:

Grading Breakdown:

Component	Weight
Homework	15%
Quizzes	5%
Exam 1	20%
Exam 2	20%
Exam 3	20%
Final Exam	20%

Letter Grade Scale:

Percentage	Letter Grade
97 - 100	A+
93 - 96	A
90 - 92	A-
87 - 89	B+
83 - 86	B
80 - 82	B-
77 - 79	C+
73 - 76	C
70 - 72	C-
67 - 69	D+
63 - 66	D
60 - 62	D-
59 and below	F

Final grades are rounded to the nearest integer before applying the scale above.

Grades are not curved.

Once you complete your exam, you will receive a 0 on any homework leading up to that exam that has not been submitted. Under special circumstances, students may request that they be allowed to submit these assignments. This is left to the discretion of the course instructor.

Students are encouraged to follow the guided deadlines in their course. However, as our courses are self-paced, students may occasionally submit several assignments in a short period of time. Please note that instructors are only expected to grade one exam per five-business-day week, and instructors are only expected to grade up to two submitted assignments per five-business-day week. Under special circumstances, students may request that additional assignments be graded. This is left to the discretion of the course instructor.

Due to the rolling enrollment structure of the NetMath program, instructor workloads vary throughout the year. During peak periods, response times and grading turnaround may be longer than usual. Students should expect significant delays in grading and instructor responses between June and August.

Communication:

You may reach out to the instructor via email or attend office hours.

If you experience consistent and significant delays in reaching your instructor, please contact instruction@netmath.illinois.edu with your concerns.

If you have non-course specific questions, you may reach out to the NetMath office. It is recommended to [review the NetMath website](#) first as it often has the answers you need.

General Inquiries: netmath@illinois.edu

Proctoring Questions: proctor@netmath.illinois.edu

Technology Questions: tech-staff@netmath.illinois.edu

Main Office Phone: [\(217\) 265-0439](tel:(217)265-0439)

Phone hours: Monday - Friday, 9am - 12pm & 1pm - 4pm CST

Textbook:

Required Textbook:

Goodman, Frederick M. (2014). Algebra: Abstract and Concrete. (Edition 2.6).
SemiSimple Press

Recommended Textbook:

Axler, Sheldon. (2025). Linear Algebra Done Right. (Edition 4). Springer.

- A good book on linear algebra, which is closely tied to our course. Some of this material is assumed as a prerequisite. The more familiarity you have with this subject the better -- in this course and broadly in life. This book is freely available online: <https://linear.axler.net/>

Gallian, Joseph A. (2017). Contemporary Abstract Algebra. (Edition 9). Cengage Learning.

- A very good alternate textbook for our course.

Dummitt and Foote. Abstract Algebra. (Edition 3). Wiley.

- A more advanced book that is self-contained, so it's possible to learn the subject from this book. It goes well beyond this course, but it's chock-full of examples and exercises, both of which form the core of the subject.

Technical Requirements:

Students are expected to have a device with an up-to-date operating system to access their course materials, reliable internet access, and must meet the requirements set by ProctorU for exam proctoring. [NetMath IT- Frequently Asked Questions](#).

Other Information:

This course features video lectures from the UIUC Fall 2021 course taught by Professor Charles Rezk and includes online lecture notes.

Policies:

Accommodations:

The University of Illinois Champaign-Urbana, is committed to ensuring that all students, including students with disabilities, do not experience barriers to learning and participating fully in class. Students who have a letter of accommodation from DRES are advised to share that with their instructor and NetMath staff at instruction@netmath.illinois.edu as soon as possible to ensure accommodation needs can be discussed and met.

Students enrolled in a degree program at another institution may refer to their home institution's student services or disability office for accommodations. Current, non-expired documentation from other institutions listing the specifics of an accommodation is acceptable and should be sent to instruction@netmath.illinois.edu.

To obtain disability-related academic accommodations, disabled students must contact Disability Resources and Educational Services (DRES) as soon as possible. To contact DRES, please visit 1207 S. Oak Street, Champaign, call [\(217\) 333-1970](tel:(217)333-1970), email disability@illinois.edu, or [visit the DRES website](#).

Academic Integrity:

The University of Illinois Urbana-Champaign [Student Code](https://studentcode.illinois.edu/) (<https://studentcode.illinois.edu/>) should also be considered as a part of this syllabus. Students should pay particular attention to Article 1, Part 4: Academic Integrity.

Academic dishonesty may result in a failing grade. Every student is expected to review and abide by the [Academic Integrity Policy](https://studentcode.illinois.edu/article1/part4/1-401/) (<https://studentcode.illinois.edu/article1/part4/1-401/>). Ignorance is not an excuse for any academic dishonesty. It is your responsibility to read this policy to avoid any misunderstanding. Do not hesitate to ask the instructor(s) if you are ever in doubt about what constitutes plagiarism, cheating, or any other breach of academic integrity.

AI Large Language Models (such as ChatGPT, Claude, Gemini, etc.) are prohibited during exams. Using these during the exam will be considered a violation of academic integrity and may incur sanctions as outlined in the Illinois Student Code. Students should be aware the exam proctoring process involves screen recording of the computer. While AI will not be strictly prohibited for homework as they can be useful tools for studying and brainstorming, students are strongly encouraged to work on the homework themselves or collaborate with peers when appropriate. Students are required to submit their own work and answers. This improves learning outcomes and best prepares students for exams. Homework is designed to help students understand the content and develop skills. Students may be unprepared for exams if there is heavy reliance on AI.

Students are expected to follow the [University guidance on intellectual property](#). Students are not to share course content outside of the course.

Campus Holidays:

Instructors are expected to respond to student communications and grade homework assignments in a timely manner. Observed Campus Holidays, illness, personal obligations, or other circumstances outside the instructor's control may affect normal grading and response time. If you experience consistent and significant delays, please contact instruction@netmath.illinois.edu with your concerns.

Extensions:

Students in this course are eligible for up to two 1-month course extensions. There is a non-refundable \$350 fee for each approved extension. [Students should review the extension guidelines for more information.](#)

FERPA:

See [FERPA – Office of the Registrar](https://registrar.illinois.edu/academic-records/ferpa/) (<https://registrar.illinois.edu/academic-records/ferpa/>) for more information on the Family Educational Rights and Privacy Act (FERPA).

Any student who has suppressed their directory information pursuant to FERPA should self-identify to the instructor to ensure protection of the privacy of their attendance in this course.

Mental Health:

Significant stress, mood changes, excessive worry, substance/alcohol misuse or interferences in eating or sleep can have an impact on academic performance, social development, and emotional wellbeing. The University of Illinois offers a variety of confidential services including individual and group counseling, crisis intervention, psychiatric services, and specialized screenings which are covered through the Health Service Fee. If you or someone you know experiences any of the above mental health concerns, it is strongly encouraged to contact or visit any of the University's resources provided below. Getting help is a smart and courageous thing to do for yourself and for those who care about you.

[Counseling Center](#) or [\(217\) 333-3704](tel:(217)333-3704)

[McKinley Health Center](#) or [\(217\) 333-2700](tel:(217)333-2700)

[National Suicide Prevention Lifeline](#) or [\(800\) 273-8255](tel:(800)273-8255)

[Rosecrance Crisis Line](#) or [\(217\) 359-4141](tel:(217)359-4141) (available 24/7, 365 days a year)

If you are in immediate danger, call [911](tel:911).

*This statement is approved by the [University of Illinois Counseling Center](#)

Sexual Misconduct Reporting Obligation:

The University of Illinois is committed to combating sexual misconduct. Faculty and staff members are required to report any instances of sexual misconduct to the University's Title IX Office. In turn, an individual with the [Title IX Office](#) will provide information about rights and options, including supportive measures, resources, the campus disciplinary process, and law enforcement options.

[Designated Confidential Employees](#): A list of the designated University employees who, as counselors, confidential advisors, and medical professionals, do not have this reporting responsibility and can maintain confidentiality.

Other information about [resources and incident reporting](#).